

Lecture Notes
on
Information and the Strategic Timing of Investments

(Revised August 2018)

You know that a firm’s decision to invest is equivalent to a decision to exercise an option (which we call a “real option”). Most analyses of real options are confined to the decisions of a single firm. Although timing decisions are still involved (for example, what is the critical price of oil at which it is optimal to develop an undeveloped oil reserve?) the decisions are “non-strategic” in the sense that we do not take into account the actions of other firms. Now we will consider some of the strategic issues that arise when other firms may also be making investment decisions that can affect the ultimate market equilibrium and the profits to the first firm. There are two types of problems that can arise, and they have opposite effects on the timing of investment:

1. The market may be large enough to support only one or two firms, or for other reasons (e.g., strong network externalities) there may be a substantial first-mover advantage. This creates an incentive to invest early and preempt your competitors. Although evolving uncertainty over future market conditions will create an option value of waiting rather than investing now, the incentive to preempt may reduce this option value, or even eliminate it entirely.
2. Sometimes the investments of your competitors can yield important information. One example of this is exploration for new undeveloped offshore oil reserves. You and three or four other oil companies might all own leases that give you the right to explore on various different tracts in, say, the Gulf of Mexico. Is it worthwhile to spend a lot of

money exploring for oil on your tracts? Because outcomes across tracts are correlated, you could benefit by waiting to see whether the other companies that explore succeed or fail in finding oil. This creates an incentive to delay investment, even beyond the option value incentive that arises from evolving uncertainty over the price of oil.

1 Pharmaceutical R&D

A nice way to think about these two opposing effects is in the context of pharmaceutical R&D. Pharmaceutical R&D is usually directed at the development of new drugs for specific therapeutic categories, e.g., a new drug to reduce cholesterol, treat depression, or attack certain infectious diseases. Typically, several pharmaceutical companies will work on the development of a new drug, all based on the same biochemical mechanism.

When developing a new drug, a pharmaceutical company faces two basic types of uncertainty. First, there is uncertainty over the cost and time involved to complete the R&D, perform the necessary clinical testing, and ultimately gain FDA approval for marketing and selling the drug. Most new drugs, in fact, never even reach the final stage of FDA approval. Second, even if drug development and clinical testing are successful, there is often uncertainty over the size and value of the market. Merck, for example, developed the first protease inhibitor for the treatment of AIDS. Prior to development, however, Merck grossly underestimated the number of patients who would take such a drug (and have their insurance companies pay for it). *Ex post*, the drug was a much greater success than anticipated.

In addition, both types of strategic timing issues arise with respect to pharmaceutical R&D. There is usually a first-mover advantage when selling a new type of drug, so that the first company to complete development and testing of the drug will get the largest share of the market, the second to enter will get a smaller share, and the third and fourth, smaller shares still. (For example, Lilly's Prozac was the first to market in the SSRI antidepressant therapeutic category, and had the largest market share; Pfizer's Zoloft was the second, and in some ways superior to Prozac, but had a smaller market share; and Paxil, the third, had a smaller share still.) This first-mover advantage creates an incentive for a pharmaceutical

company to accelerate its investment in drug development.

On the other hand, firms can learn from each other's experience about the difficulty of actually completing the R&D and making it through the various stages of testing, as well as the ultimate size of the market and hence the value of a new drug. This creates an incentive to delay drug development or invest more slowly: Let the other guy find out how difficult the job is, and then we can decide whether it makes sense to go forward. Also, if the competitor is successful in developing a new type of drug, it will have to educate doctors (and patients) about the virtues of the new drug. This, too, creates an incentive to wait and invest more slowly.

Thus there are counteracting incentives. On the one hand, there is an incentive to move quickly in order to preempt and be the first to market. But on the other hand, there is an incentive to wait, learn from the experience of other companies, and let the first mover educate doctors about the new type of drug.

How can pharmaceutical companies balance these incentives and determine the optimal timing of their R&D programs? Clearly, they need to estimate the extent of first-mover advantage. First-mover advantage in pharmaceutical markets arises largely from *brand-specific network externalities*. Doctors will be more willing to prescribe, and patients more willing to take, a drug that has a large market share because that share conveys positive information about "accepted practice," as well as efficacy. Estimating the extent of these externalities is difficult, but recent statistical studies have begun to provide useful information. (Surprisingly, for many therapeutic categories, these externalities—and hence any first-mover advantage—are not as large as one might have thought.)

The brand-specific network externality must be balanced against a possible *product-specific* network externality. For any particular type of drug, both doctors and patients will be more willing to use the drug if a large number of other patients have taken or are taking a drug. In other words, doctors are more willing to prescribe, and patients to take, a type of drug if that type of drug has been "accepted," and "acceptance" is best measured by the number of other people that have taken or are taking that type of drug.

Thus firms need to assess the nature and extent of uncertainty over the completion of

R&D programs and over market size assuming a successful completion. And they need to evaluate potential brand-specific and product-specific network externalities. This is something that pharmaceutical firms have had to do frequently, so although difficult, it is not at all alien to them. What is more difficult is assessing what they can learn from the activities of their competitors, and how to use that in making a strategic timing decision. We will address aspects of that issue below.

2 Learning from Others

I will assume here that the reader is already familiar with the basic ideas behind the “real options” approach to investment. (Those ideas are set forth in Chapter 2 of A. Dixit and R. Pindyck, *Investment Under Uncertainty*, which is in the 15.013 readings packet, and we will go over them in class.) Here we will consider what can happen if there are *two* firms considering an investment, and investing by one firm can yield information to the other.

Suppose that your firm and another firm are both considering producing digital widgets. The problem is that neither of you knows how much consumers are willing to pay for these widgets. Right now, you think they would pay either \$50 per widget, or \$150, each with equal probability. You will not be able to find out consumers’ willingness to pay until you—or the other firm—actually makes an investment and begins producing the widgets.

Each firm can invest in one unit of capacity at a cost of \$800. Note that at this point there is no value of preemption—we are assuming that there are enough potential buyers so that once you have made the investment, you can sell one widget per year, whether or not the other firm is also producing and selling widgets. The only concern is the price that can be charged. Hence, for each firm, the net present value of investing now is:

$$\text{NPV}_i^{\text{NOW}} = -800 + \sum_{t=0}^{\infty} 100/(1 + R)^t \quad (1)$$

Note that \$100 is the *expected* price that consumers would be willing to pay. We will assume that the discount rate, R , is ten percent (because that’s a round number), so that this NPV becomes $\text{NPV}_i^{\text{NOW}} = -800 + 1100 = \300 .

Suppose Firm 2 is going to invest now. Should Firm 1 wait a year before deciding whether to invest? If it waits, it will only invest if it learns that consumers are willing to pay \$150 per widget. So assuming Firm 2 will indeed invest now, the NPV for Firm 1 from waiting is:

$$\text{NPV}_1^{\text{WAIT}} = \frac{1}{2} \left[-\frac{800}{1.1} + \sum_{t=1}^{\infty} 150/(1.1)^t \right] = \$386 \quad (2)$$

Hence, in this situation it is better to wait.

The problem here is that Firm 2 is thinking the same thing, and would also like to wait for Firm 1. Suppose that as a result, neither firm invests now, and both wait a year, hoping (in vain) that the other firm will invest. If at the end of the year, both firms then go ahead and invest (without the benefit of any knowledge about the market), the NPV calculated as of today will be:

$$\text{NPV}_i^{\text{WAIT}} = 300/1.1 = \$273 \quad (3)$$

We thus have a gaming situation, the payoffs for which are shown below. Note that each firm would like the other one to invest first, but in all likelihood both firms will wait a year, and in the end gain nothing in the way of new information. Assuming there is no longer any further possibility of waiting, they will then both invest, and be worse off than they would have been had they simply invested now. Also note that if the firms could collude, they would probably agree to toss a coin to see who will invest first. In that case, each firm would have an expected NPV of $\frac{1}{2}(300) + \frac{1}{2}(386) = \343 .

		<u>Firm 2</u>	
		Now	Wait
<u>Firm 1</u>	Now	300, 300	300, 386
	Wait	386, 300	273, 273

Assuming that collusion and agreement to toss a coin is not possible, how would you play this game if you were Firm 1? Note that you are in a *war of attrition*—each firm is hoping

that the other will “blink” first, where in this case “blinking” means investing (not dropping out). Hence, depending on your expectations regarding the other firm, it may be rational to invest now, or it may be rational to wait.

What you might do in this case is assign a probability to the outcome that Firm 2 will invest now. Suppose that probability is p . Then, your expected NPVs for investing now is:

$$\text{NPV}_1^{\text{NOW}} = 300 , \quad (4)$$

and your expected NPV for waiting is:

$$\text{NPV}_1^{\text{WAIT}} = (p)(386) + (1 - p)(273) = 273 + 113p \quad (5)$$

Hence it is better to wait as long as $273 + 113p > 300$, or $p > .24$. The question then becomes, is it reasonable to think that the probability that Firm 2 will invest now is greater than .24? That is a difficult question — it depends not only on the characteristics of Firm 2’s managers, but also on what those managers are thinking about you and your characteristics.

Of course, there is no reason for this process to stop at the end of one year. Suppose that you and the other firm have both decided to wait a year. At the end of the year, both of you observe that (sadly) no one has invested. You are now in the very same situation you were in before. Should you wait another year, or go ahead and invest now? And, of course, if you both wait another year, the process will then repeat itself.

In this war of attrition it is possible for a very long time to go by with neither firm investing. This is indeed likely, unless some other element is introduced to push the firms towards early investment. Take, for example, the case of undeveloped off-shore oil reserves. The payoffs from developing such reserves (by building platforms and drilling production wells) are very uncertain, because there is uncertainty over costs and over the quantity of oil that can be extracted (as well as over the future price of oil). Hence there is an incentive for each firm to wait before developing a reserve. Each firm can learn about the likely quantity of oil that can be extracted by watching other nearby firms, with no fear of being “preempted,” because the world price of oil is independent of what these firms do. In this case the outside element that encourages early investment is a “relinquishment requirement”

imposed by the government—the firms will lose their rights to the oil reserves if they do not begin development within a certain period of time.

Another element that can induce one or both firms to invest early is the fear of preemption. In our widget example above, we assumed that each firm’s demand is independent of what the other firm does. But suppose that by building enough capacity, each firm could gain a first-mover advantage that would reduce the potential returns from investing by the other firm. In this case, the incentive to preempt (and avoid being preempted) might outweigh the incentive to wait for information.

We saw how this might work in the context of pharmaceutical markets. In those markets there are significant network externalities associated with a therapeutic category of drug (i.e., a type of drug), and also with a *brand* of drug within a therapeutic category. However, recent research has suggested that the brand-level network externalities may be weak in many cases. (The strength of any network externalities at the level of a therapeutic category or the level of a specific brand is likely to depend on the particular type of drug.) If brand-specific network externalities were important, this would create an incentive for firms to invest early and try to preempt. However, if brand-specific network externalities are small or nonexistent, it may be preferable to move slowly and be the second entrant in the market (as was Glaxo when it introduced Zantac). Hence, for strategic planning purposes, it is essential to evaluate the strength of these network externalities.

3 First-Mover Advantage and Investment Timing

Let us now put aside the possibility of learning from the investment activities of others, and simply examine the implications of first-mover advantage. We will use the same simple two-period framework that we used in the previous section. Now, however, we will assume that information is revealed by “nature,” and not by the activities of a competing firm.

Once again, suppose that *two* firms can invest. The cost of the investment for either firm is \$800. The first to market can sell one widget per year forever, at a price P . Currently, $P = \$100$; next year P will be \$50 or \$150 with equal probability. The discount rate is 10%.

Thus the NPV for the firm that enters now *and* is the first to market is given by eqn. (1).

What about the second firm to market? Suppose that firm can also sell one widget per year forever, but only at a price βP , with $\beta < 1$. Thus if the firm that is second to market enters while the price is still \$100, its NPV is $-800 + 1100\beta$.

If one firm invests now and the other firm waits, the second firm will have an NPV given by:

$$\text{NPV}_2^{\text{WAIT}} = \frac{1}{2} \left[-\frac{800}{1.1} + \sum_{t=1}^{\infty} 150\beta / (1.1)^t \right] = -\$364 + \$750\beta \quad (6)$$

Finally, if both firms wait, the who manages to preempt will have an NPV of \$386, while the second to market will have an NPV of $-\$364 + \750β .

The payoff matrix for the two firms is shown below.

		<u>Firm 2</u>	
		Now	Wait
<u>Firm 1</u>	Now	300, $-800 + 1100\beta$ OR $-800 + 1100\beta$, 300	300, $-364 + 750\beta$
	Wait	$-364 + 750\beta$, 300	386, $-364 + 750\beta$ OR $-364 + 750\beta$, 386

Note that if both firms invest now, the first to market receives an NPV of \$300, and the second to market receives an NPV of $-\$800 + \1100β . We don't know which firm will reach the market first, so there are two possible outcomes for the (N_1, N_2) strategies, and likewise there are two possible outcomes for the (W_1, W_2) strategies.

If it were desirable to preempt, each firm could, in principle, spend more to complete the investment and get to the market first. As we have seen when we studied "winner-take-all" markets, this could lead to a destructive race, or war of attrition, where both firms lose

money. To keep things as simple as possible, however, let us ignore this possibility. Suppose that the only investment allowed is the \$800 to build the widget factory, and if both firms invest at the same time, the one that gets to market first is determined randomly, e.g., by a coin toss. Thus if both firms invest now, the expected NPV for each firm is

$$\text{NPV}_i^{\text{NOW}} = \frac{1}{2}(300) + \frac{1}{2}(-800 + 1100\beta) = -250 + 550\beta \quad (7)$$

If both firms wait, the expected NPV for each firm is

$$\text{NPV}_i^{\text{WAIT}} = \frac{1}{2}(386) + \frac{1}{2}(-364 + 750\beta) = 11 + 375\beta \quad (8)$$

We can now write the payoff matrix in terms of *expected* NPVs. This is shown below.

		<u>Firm 2</u>	
		Now	Wait
<u>Firm 1</u>	Now	$-250 + 550\beta,$ $-250 + 550\beta$	$300,$ $-364 + 750\beta$
	Wait	$-364 + 750\beta,$ 300	$11 + 375\beta,$ $11 + 375\beta$

There are several things that we can observe from this payoff matrix:

1. First, for any value of β , waiting by both firms dominates investing now (in expected value terms). Also, for any value of β , waiting by both firms yields a positive expected NPV. The reason is that both firms will end up investing only if the price of widgets goes up to \$150. If β is equal to, say, .40, the firm that arrives in the market second will have an *ex post* negative NPV, but the *ex ante* expected NPV is positive.

2. Suppose Firm 2 is going to invest now (and thus try to preempt). Might Firm 1 still want to wait? To answer this, just compare the expected payoffs from waiting versus investing now. Clearly, Firm 1 should wait if

$$-364 + 750\beta \geq -250 + 550\beta$$

That is, the firm should wait if β is greater than or equal to .57.

What can we learn from this? First, if the gains from preemption are very large (i.e., β is small), neither firm will invest now, unless it has a means of preemption. The reason is that if both firms try to invest at the same time, the ex ante expected NPV is negative. However, even if the gains from preemption are small (e.g., $\beta = .8$), it is better to wait. The reason is that the value of waiting exceeds the gains from preemption. Of course, in this case *both* firms would want to wait. (For example, if $\beta = .8$, (W_1, W_2) yields an expected NPV of \$311 for Firm 2, while (W_1, N_2) yields \$236 for Firm 2.)

Note that unless there is some action that one firm can take to preempt (and the other can't), *the value of early entry can be separated from the value of waiting and learning*. In other words, the game theoretic problem can be separated from the real options problem. Thus, a firm can begin by analyzing the pure value of waiting, ignoring preemption, and then given the resulting NPVs, analyze the gaming situation, taking preemption into account.

4 Bubbles and Informational Cascades

Bubbles are a form of learning from others: You and other investors (maybe speculators is a better word) observe that the price of land in Iowa has been rising rapidly, so clearly many other people think that land in Iowa is a good investment. As a result, you and others buy land in Iowa, pushing the price up further. You have all learned something from the behavior of others, and that creates a bubble. When does the bubble burst? At some point, some investors decide to get out of the market, so they sell their land and the price begins to fall. You and others observe this, so you also sell, pushing the price down further.

Does this mean that if you observe something that looks like it might be a bubble, you should stay away? Maybe not. It depends on what is driving the price increases.

In particular, we want to distinguish *rational* from *irrational* bubbles. To understand the difference, let's elaborate a bit on that land in Iowa. Suppose land prices are rising, and you, like others, observe that many people are buying land. Furthermore, you read a report that argues that land prices will keep rising because more and more people want to move to Iowa. Should you also buy land? Maybe.

An *irrational bubble* is one in which the expected NPV of investing is less than or equal to zero. This might be the case if the report you read was poorly researched, or has already been read by everyone else and thus is fully incorporated in the price, and you have no reason to expect that the other people buying land know more than you do. Put simply, ask yourself the following question: Can you demonstrate (i.e., argue intelligently and coherently) that investing in land has a positive NPV? (Simply claiming that you will get out at a time before the price starts dropping — without explaining how you will know when that time is — is not sufficient.) If not, the bubble, at least as far as you are concerned is irrational. In this case, learning from others has no value.

A *rational bubble* is one in which the expected NPV of investing is positive. Again, you must ask whether you can indeed demonstrate that the NPV is positive. In this case learning from others has value. But what might make learning from others valuable and generate a positive NPV? One possibility is an informational cascade. But as we will see, although an informational cascade can lead to a positive NPV, the associated risk might be enormous.

4.1 Informational Cascades

Learning from others sometimes leads to unfortunate results. Suppose you are considering investing in the stock of Ajax Corp., which is currently trading at \$20 per share. Ajax is a biotech company that is working on a radically new approach to the treatment of chronic boredom (a disease that sometimes afflicts students of economics). You find it difficult to evaluate the company's prospects, but \$20 seems like a reasonable share price. But now you see that the price is increasing — to \$21, \$22, then a jump to \$25 per share. In fact, some friends of yours have just bought in at \$25. Now the price reaches \$30. Other investors must know something. Perhaps they consulted biochemists who can better evaluate the

company's prospects. So you decide to buy the stock at \$30. You decided that there was positive information in the actions of other investors, and you acted accordingly.

Was buying the stock of Ajax at \$30 a rational (or "rationalizable") decision? It certainly might be. After all, it is reasonable to expect that other investors tried to value the company as best they could, and that their analyses might have been more thorough or better-informed than yours (even though they are not Sloan graduates). Thus the actions of other investors could well be informative and lead you to rationally adjust your own valuation of the company. In fact, we would expect that to be the case if the stock market is reasonably efficient. Likewise, the fact that other investors are buying up real estate in downtown Oshkosh could lead you to rationally conclude that the future of Oshkosh is quite bright indeed, so that you should also pick up some downtown real estate now, before it doubles or triples in price.

Note that in these examples, your investment decisions are based not on fundamental information that you have obtained (e.g., regarding the likelihood that Ajax's R&D will be successful or regarding real estate supply and demand conditions in Oshkosh), but rather on the investment decisions of others. And note that you are implicitly assuming that: (i) these investment decisions of others are based on fundamental information that *they* have obtained; *or* (ii) these investment decisions of others are based on the investment decisions of others still, which are based on fundamental information that *they* have obtained; *or* (iii) these investment decisions of others are based on the investment decisions of others still, which in turn are based on the investment decisions of still more others, which are based on fundamental information that *they* have obtained; *or* ... etc., etc. You get the idea. Maybe the "others" at the end of the chain based their investment decisions on weak information that was no more informative than the information you started with when you began thinking about Ajax and Oshkosh. In other words, your own investment decisions might be the result of an *informational cascade* — actions based on actions based on actions ..., etc., driven by very little fundamental information. You might think of this as simply a "bubble" or "herd behavior," but it is important to understand how it arises, and how it can end (often unhappily for investors at the end of the chain).

4.2 A Simple Example

We want to distinguish between actions based on the arrival of fundamental information (which I will refer to as a “signal”) versus actions based on the actions of others, which might have some eventual link to the arrival of fundamental information. A simple example will help to clarify the difference, and illustrate how actions based on actions can lead to an informational cascade.¹

Let’s return to downtown Oshkosh. Suppose individuals are deciding in sequence whether to take an action — in this case, buy some real estate. If an individual acts, the ultimate payoff will be the fundamental value V of a piece of real estate, which is either 1 or -1 , and initially the probability of either payoff is $\frac{1}{2}$. (The payoff from not acting is zero.) Individuals receive *signals*, which can be either *High* (H) or *Low* (L). If in fact $V = 1$, the signal will be H with probability $p > \frac{1}{2}$ and L with probability $(1 - p) < \frac{1}{2}$, but if in fact $V = -1$, the signal will be H with probability $(1 - p) < \frac{1}{2}$ and L with probability $p > \frac{1}{2}$. In other words, a signal is informative, but it doesn’t eliminate all of the uncertainty. Note that if you receive one signal and it is H, your posterior probability that $V = 1$ becomes $p > \frac{1}{2}$, but if the signal is L, your posterior probability that $V = 1$ becomes $(1 - p) < \frac{1}{2}$.²

Observable Signals. Now suppose that a new signal comes every week, and that all past signals are observed by all potential investors. In other words, information keeps accumulating, and is available to everyone. What will happen? As the number of signals

¹This example is drawn from S. Bikhchandani, D. Hirschleifer, and I. Welch, “Learning from the Behavior of Others: Conformity, Fads, and Informational Cascades,” *Journal of Economic Perspectives*, Summer 1998, **12**, 151–170.

²We have made use of *Bayes Theorem*, and will continue to make use of it in what follows. For those of you who might have forgotten what you learned in statistics, Bayes Theorem tells us how to calculate the probability of event A given that event B has occurred (i.e., the *posterior probability of A given B*). Letting P represent probability, and $P(A|B)$ represent the probability of A given B, Bayes Theorem says

$$P(A|B) = \frac{P(A)P(B|A)}{P(B)}$$

Thus the posterior probability that $V = 1$ given a high signal is

$$P(V = 1|H) = \frac{P(V = 1)P(H|V = 1)}{P(H)} = \left(\frac{1}{2}\right)(p) / \left(\frac{1}{2}\right) = p$$

increases, the uncertainty over the true fundamental value V is continually reduced, so that all investors will eventually settle on the correct choice — they will buy real estate if in fact $V = 1$ and they will not buy any if in fact $V = -1$. (If the signals are observed with noise, information will accumulate more slowly, but it will still eventually draw investors to the same correct decision.)

Observable Actions. Suppose instead that each individual receives one signal, and beyond your own signal, you can only observe the *actions* of other individuals. It is easy to see that this can lead to an informational cascade in which many people act (buy real estate) even though in fact $V = -1$, or alternatively many people do not act even though in fact $V = 1$.

Consider a sequence of risk-neutral individuals, labeled A, B, C, etc. We want to know what each individual will do given his or her own signal, and given the observed actions of his or her predecessors.

- Clearly A will act if his signal is H, but will not act if his signal is L. (His expected NPV is positive if the signal is H and negative if it is L.) And note that all other individuals can infer A's signal perfectly from his decision; if he acted he must have observed H, and if he didn't he must have observed L.
- Suppose A acted. Now what should B do? Clearly B should act if her signal is H.³ However, if her signal is L, her posterior probability that $V = 1$ is $\frac{1}{2}$, so she is indifferent. We will assume that in this case she flips a coin to decide what to do.
- Individual C now faces three possible situations:

³We can again make use of Bayes Theorem. The probability that $V = 1$ given two signals of H is

$$P(V = 1|H, H) = \frac{P(V = 1)P(H, H|V = 1)}{P(H, H)}$$

Note that $P(V = 1) = \frac{1}{2}$, $P(H, H|V = 1) = p^2$, and $P(H, H) = P(H|H)P(H) = \frac{1}{2}P(H|H)$. Finally, $P(H|H) = P(V = 1|H)P(H|V = 1) + P(V = -1|H)P(H|V = -1) = p^2 + (1 - p)^2$. Therefore

$$P(V = 1|H, H) = \frac{p^2}{p^2 + (1 - p)^2}$$

If $p = .6$, this probability is .69; if $p = .8$, this probability is .94.

1. A and B both acted. In this case, C will act, even if his signal is L. You can check that no matter what signal C receives, given that both A and B have acted, his NPV of acting is positive — even though B may well have flipped a coin after receiving a low signal.⁴
 2. A and B both rejected the investment. In this case, C will reject, no matter which signal he receives.
 3. A acted and B did not, or vice versa. Then C will act only if his signal is H.
- We will focus on the first situation: A and B both acted, and thus C acts even if his signal is L. In this case, what will D do? She will act, no matter what signal she receives. Likewise, E, F, etc., will all act.

We now have an informational cascade. It is quite possible that A, *and only A*, received a signal of H, and that all subsequent individuals received a signal of L. If D, E, etc. could have observed that B and C received signals of L, they would not have acted. But all they can observe is the *actions* of their predecessors. Everyone is acting rationally (expected NPVs are positive) even though no new information is being produced.

So, the price of real estate in downtown Oshkosh keeps going higher and higher. You observe that all 15 real estate investors who visited Oshkosh bought some property, so you — quite rationally — jump on the bandwagon and buy property yourself, pushing the price higher still.

Assuming that in fact $V = -1$, how does this process end? In the simple model described above, it only ends when we run out of investors. But in reality it probably ends when some new kind of signal becomes available to at least some investors. Perhaps a few smart investors begin to notice that there are hardly any people living in Oshkosh, and that no tourist would ever want to visit the town. Perhaps those investors, who now have new signals of L, share those signals, and then update the probabilities and expected NPVs of investing.

⁴It involves some algebra, but using Bayes Theorem, you can check that the probability that $V = 1$ given that A acted (which means his signal was H), B acted (which means that either her signal was H or it was L and she flipped a coin), and C's signal was L is $(p + 1)/3$. Because $p > \frac{1}{2}$, this probability is greater than $\frac{1}{2}$, so that C's NPV of acting is positive.

The investors then start to sell their property. Other investors observe these actions, and — quite rationally — also sell. And the price of real estate in downtown Oshkosh plummets.

4.3 What to Do?

Our little story about real estate in Oshkosh shouldn't seem that far-fetched. There are plenty of real-world examples that followed this pattern:

- During the late 1970s and early 1980s, large banks made loans to Latin American countries, even though it wasn't clear that those loans could be repaid. Each bank did its homework (and received a “signal”), but also watched what other banks were doing. Since banks make money by making loans, and other banks were making loans, lending seemed to have a positive NPV. *Ex post*, the NPV was negative—very negative.
- Another example is the oil-based real estate boom in Texas and Oklahoma during the 1980s, along with loans to any company with an oil- or gas-related project. Oil prices had peaked in 1982, and some “signals” pointed to continuing increases in price. Then in 1986 the price of oil plummeted, and the banks lost lots of money.
- Don't forget the housing bubble. Housing prices in the U.S. increased rapidly from 1998 to 2007, especially in states like Florida, Nevada, Arizona, and California. Early “signals” pointed to demographic shifts that would surely lead to greater demand for housing, and then investors followed in the footsteps of other investors. The bubble burst in 2008, and prices fell sharply. And the U.S. is not unique: the housing bubble in Spain was far worse, and China has experienced its own housing bubble.
- Then there is Bitcoin (and the many other cryptocurrencies). Unlike a share of Apple stock, or a fiat currency like the U.S. dollar, Bitcoin has no intrinsic value. It can serve as a currency only insofar as many other people are willing to accept it and use it as a currency (and so far its use as a currency is very limited). As you can see from Figure 1, in the space of one year its price went from about \$100 to over \$20,000. You decide whether this is a bubble, rational or otherwise.



Figure 1: Bitcoin Price, July 2013 to July 2018

- Finally, recall our discussion of WebMD. Around the year 2000 it was viewed by many as the “Next Big Thing,” and it had a stock market value of around \$50 billion (in 2018 dollars). But it turned out not to be such a “big thing,” and its market value dropped to about \$0.5 billion, i.e., a hundredth of its peak value.

So what’s the lesson from this story? Remember that the investors in Oshkosh who observed the actions of other investors were acting rationally — the NPVs were always positive. But we didn’t say much about the *riskiness* of their investments. (We didn’t need to worry about that because I assumed that the individuals were all risk-neutral.) Compare once again what happens with observable signals versus observable actions. With observable signals, uncertainty is reduced as more and more signals arrive, i.e., as more fundamental information accumulates. With observable actions, on the other hand, the informational

cascade leads to no reduction in uncertainty. Each individual's NPV remains positive, but the uncertainty confronting individual C is the same as for D, for E, and so on. Thus the fact that 15 people bought real estate in Oshkosh is no more informative (and should be no more comforting) than the fact that 3 people did.

Does that mean you (the 16th investor) shouldn't buy real estate in Oshkosh? Not at all. But you should understand just how much (or how little) information your decision is based on. And you should understand how rational decisions based on the actions of others can involve much more risk than decisions based on the accumulation of fundamental information.

4.4 More on Housing Prices

Let's take another look at the housing bubble in the U.S. Figure 2 shows the Case-Shiller Housing Price Index in nominal and real terms, for 1987 through 2016. The run-up in prices from 2000 to 2006 was impressive, as was the sharp price decline during 2007–2008. Would it have been irrational to invest in housing in, say, 2005? (By “invest,” I mean buy houses purely as an investment, not as a place to live.)

To answer this question, let's look at house prices in different cities, instead of the U.S. as a whole. Figure 3 shows the housing price index for each of five cities: Los Angeles, Miami, Las Vegas, New York, and Cleveland. Consider Miami, which of the five had the second-highest price run-up (and second-highest decline). Suppose the year is 2005, and you are considering investing in Miami real estate, perhaps by buying five or ten condos. Would this have been irrational, or could you have argued that the NPV was positive?

At the time, studies of the Miami housing market pointed to continued strength. Had you done your own study, you might have concluded that prices were likely to continue rising for some time because: (a) A large segment of the U.S. population has reached or will soon reach retirement age and will want to live somewhere warm (if not for the whole year, at least during the winter). This would drive the demand for condos. (b) A growing number of people in South and Central America were buying houses or condos in Miami, as an investment and/or to have a place to possibly move to in the future. Given that your

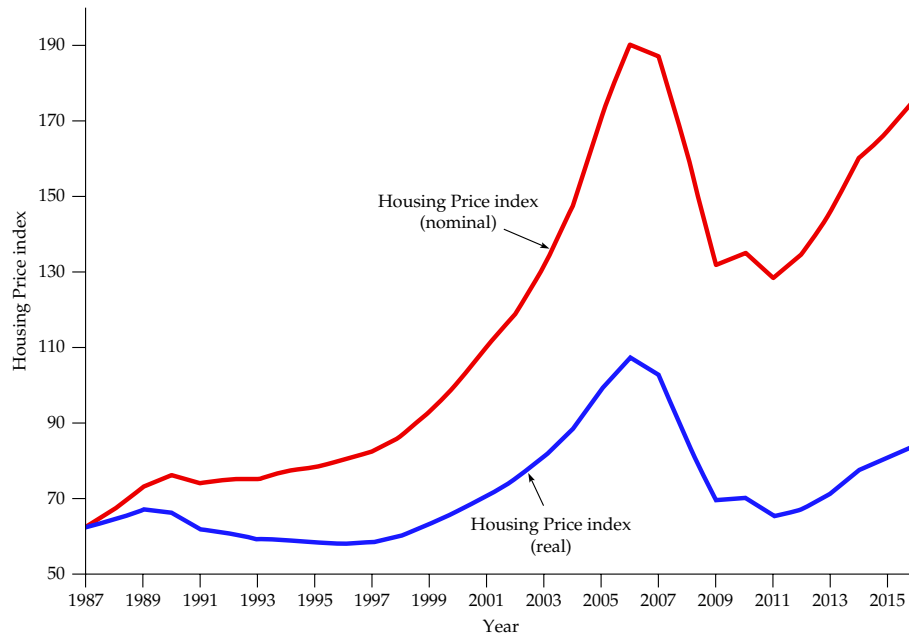


FIGURE 19.4
S&P/CASE-SHILLER HOUSING PRICE INDEX

The Index shows the average home price in the United States at the national level. Note the increase in the index from 1987 to 2006, and then the sharp decline.

Figure 2: Case-Shiller Housing Price Index

own study gave a “high” signal, and clearly at least some other people had done studies that gave “high” signals, it would have been easy to conclude that the Miami housing market presented a positive NPV investment opportunity. Hopefully, however, you would have also considered the risk involved.

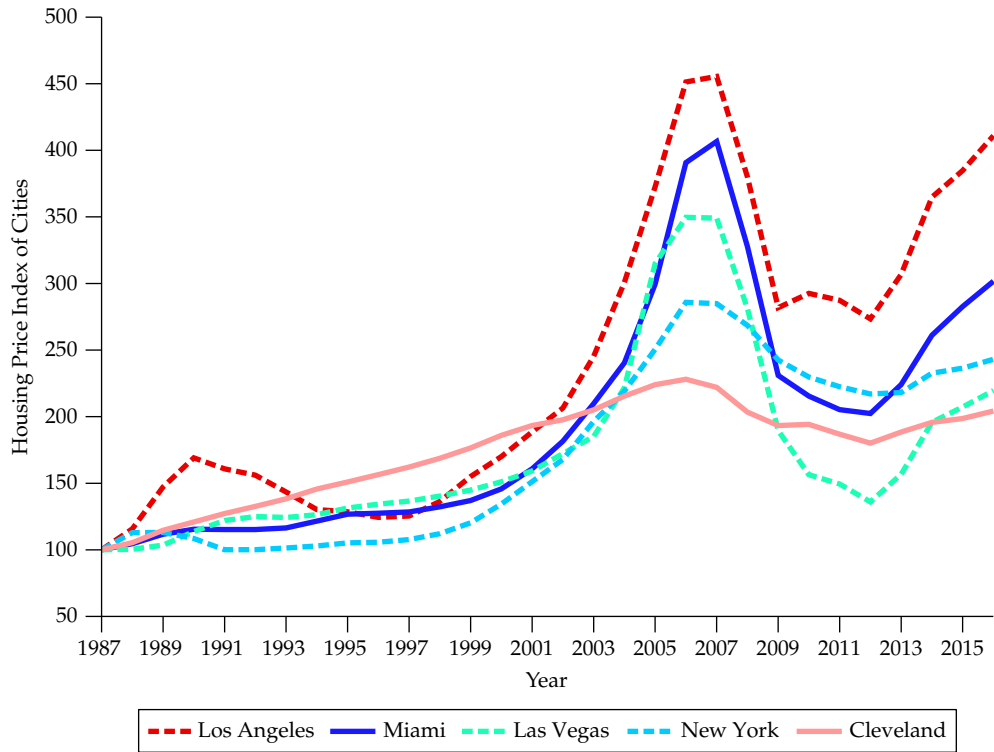


FIGURE 19.5
S&P/CASE-SHILLER HOUSING PRICE INDEX FOR FIVE CITIES

Figure 3: Housing Prices in Different Cities