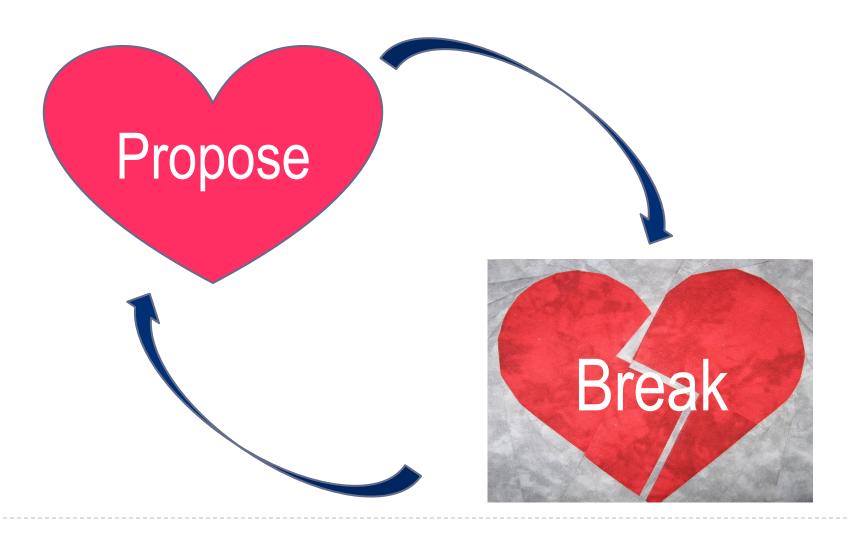
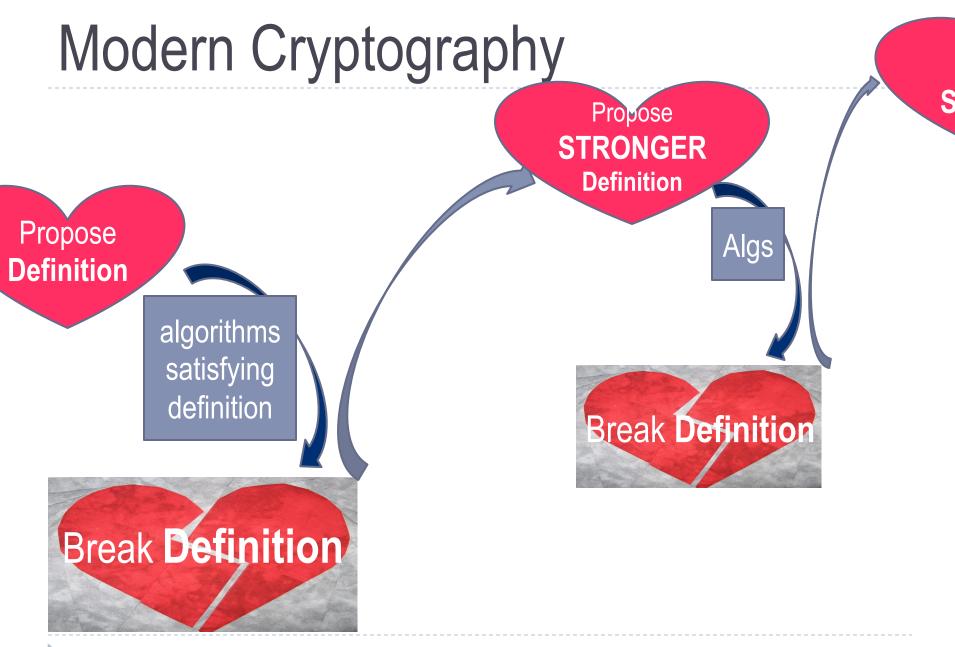
#### The State of the Art

Cynthia Dwork, Microsoft Research

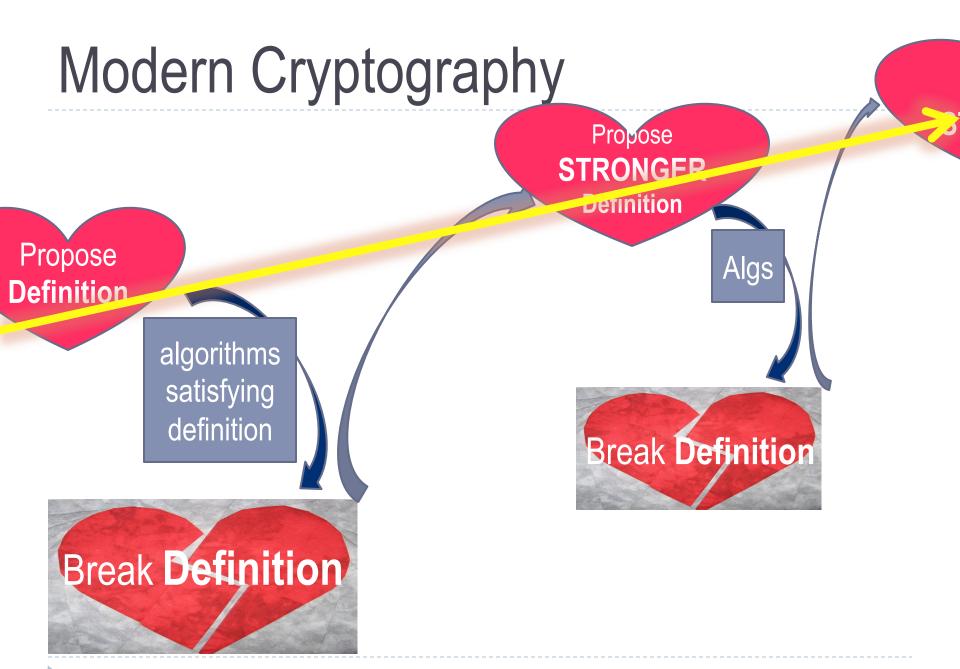
# Pre-Modern Cryptography





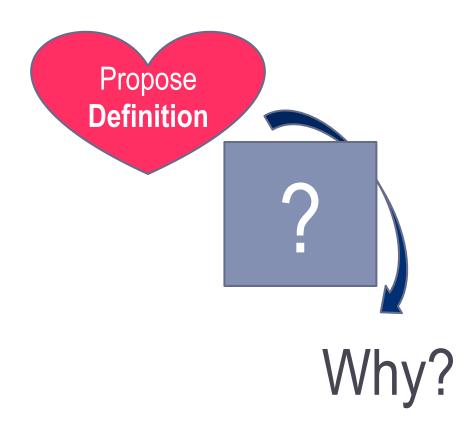


[GoldwasserMicali82,GoldwasserMicaliRivest85]



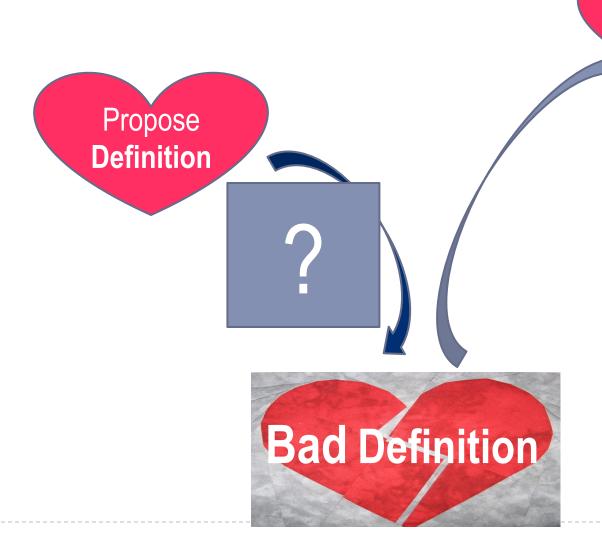
[GoldwasserMicali82,GoldwasserMicaliRivest85]

# No Algorithm?





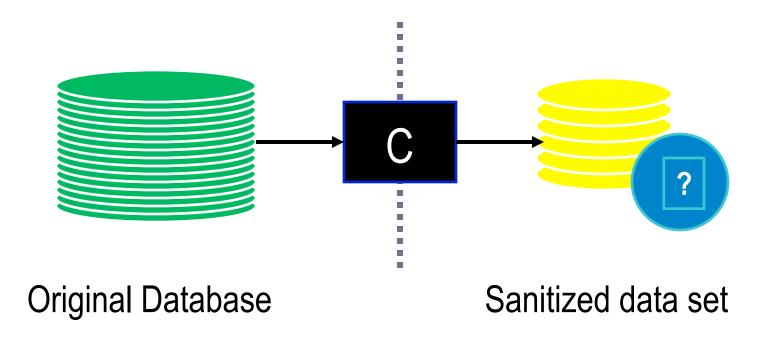
**Provably No Algorithm?** 



Propose
WEAKER/DIFF
Definition

Alg / ?

### The Privacy Dream



Census, financial, medical data; OTC drug purchases; social networks; MOOCs data; call and text records; energy consumption; loan, advertising, and applicant data; ad clicks product correlations, query logs,...



### Fundamental Law of Info Recovery



"Overly accurate" estimates of "too many" statistics is blatantly non-private

Remove "personally identifying information"



Name sex DOB zip symptoms previous admissions medications family history



Remove "personally identifying information"



Name sex DOB zip symptoms previous admissions medications family history



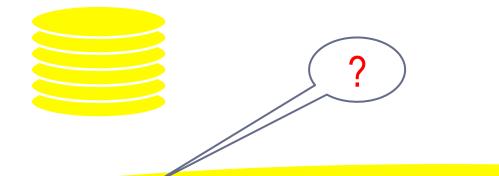
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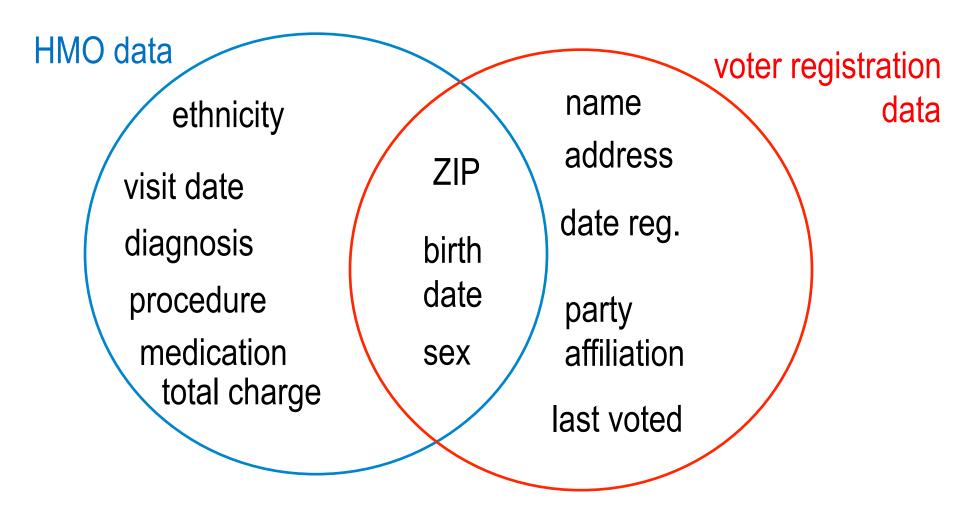


Name sex DOB zip symptoms previous admissions medications family history

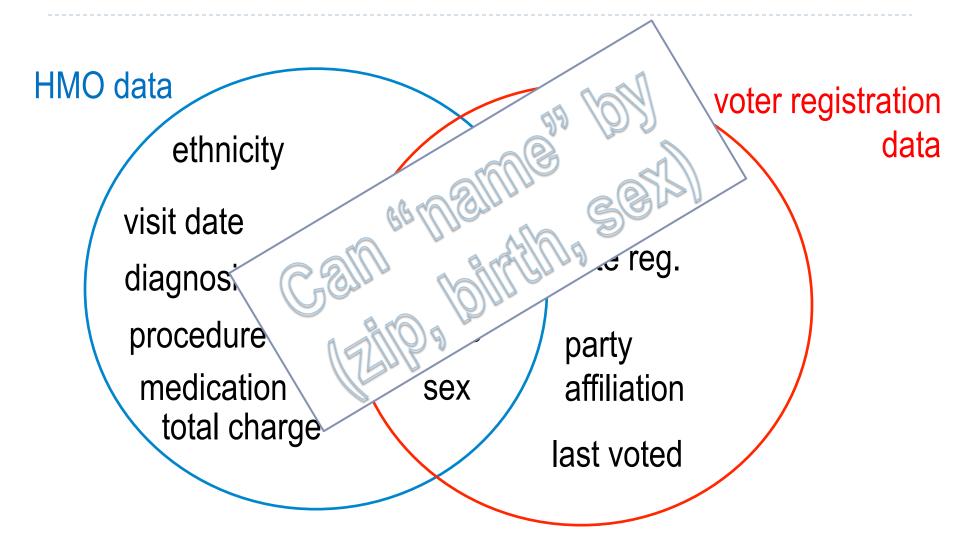
...



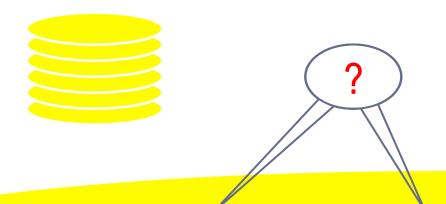
### William Weld's Medical Records



#### William Weld's Medical Records



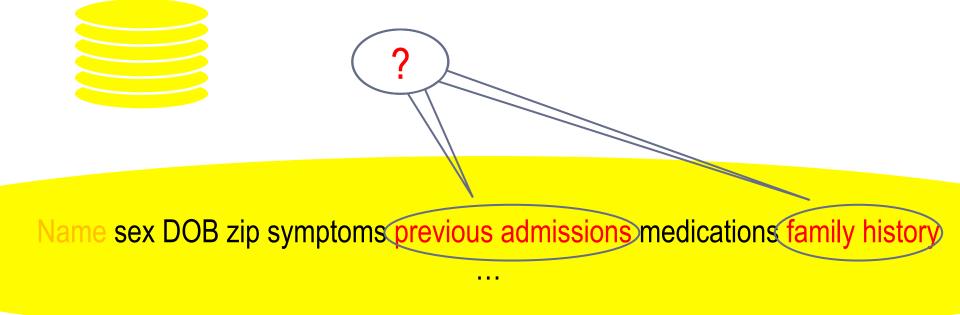
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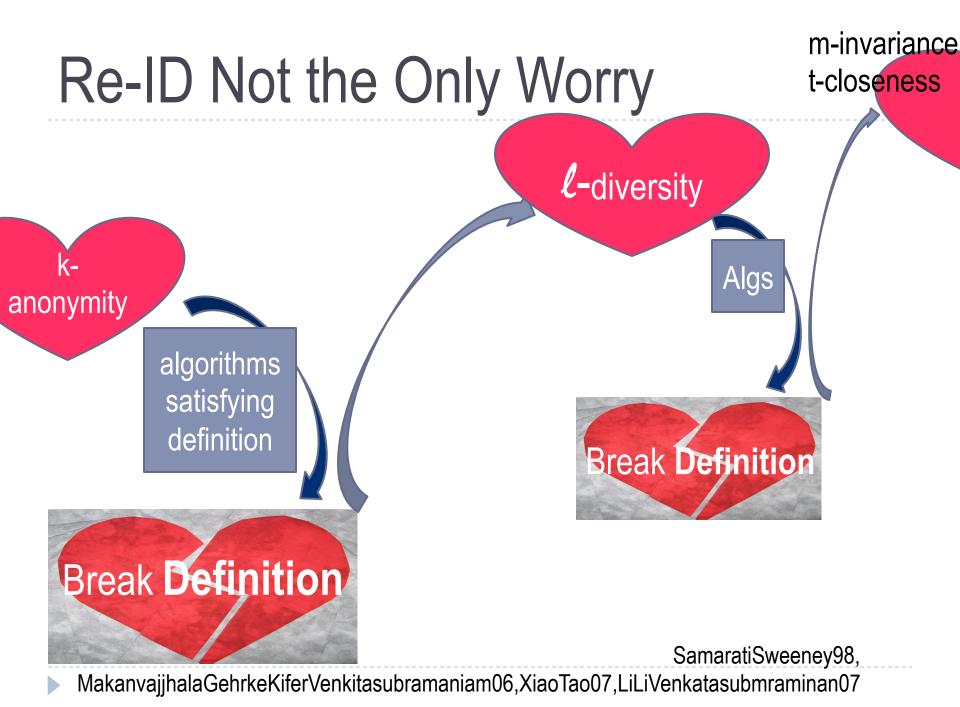


#### NETFLIX

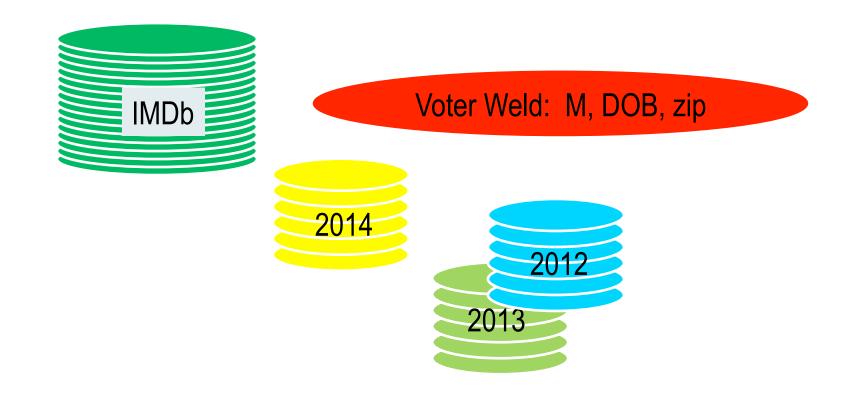
#### **Netflix Prize**







## Culprit: Diverse Background Info





## Billing for Targeted Advertisements







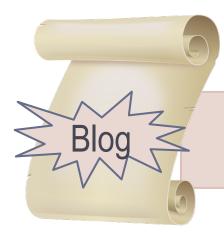






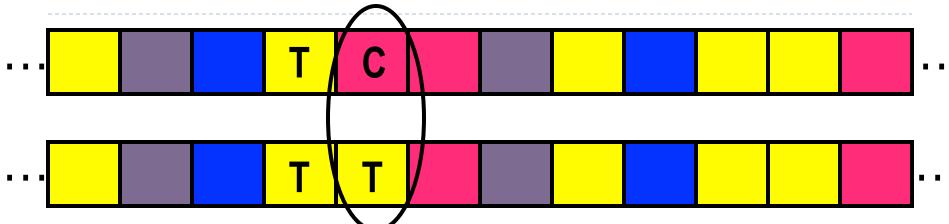
#### **Product Recommendations**

- X's preferences influence Y's experience
  - Combining evolving similar items lists with a little knowledge (from your blog) of what you bought, an adversary can infer purchases you did not choose to publicize

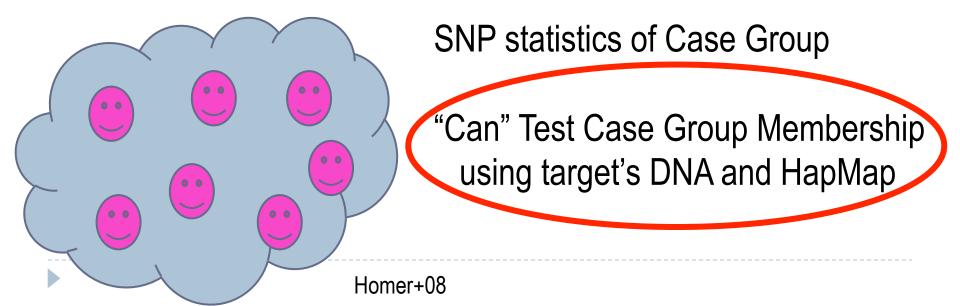


People who bought this also bought...

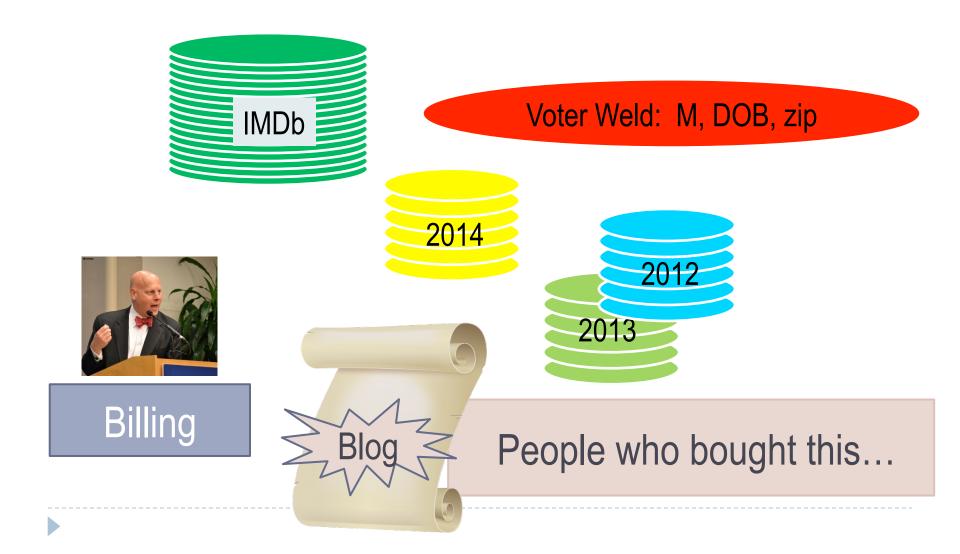




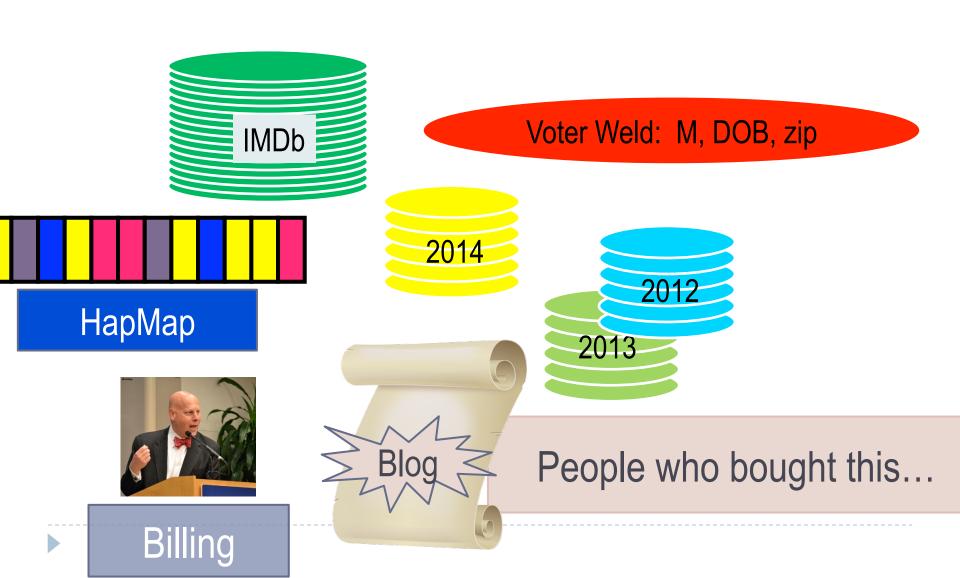
SNP: Single Nucleotide (A,C,G,T) polymorphism



### Culprit: Diverse Background Info



## Culprit: Diverse Background Info



### How Should We Approach Privacy?

"Computer science got us into this mess, can computer science get us out of it?" (Sweeney, 2012)



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- "Computer science got us into this mess, can computer science get us out of it?" (Sweeney, 2012)
- Complexity of this type requires a mathematically rigorous theory of privacy and its loss.



### How Should We Approach Privacy?

- "Computer science got us into this mess, can computer science get us out of it?" (Sweeney, 2012)
- Complexity of this type requires a mathematically rigorous theory of privacy and its loss.
  - We cannot discuss tradeoffs between privacy and statistical utility without a measure that captures cumulative harm over multiple uses.
  - Other fields -- economics, ethics, policy -- cannot be brought to bear without a "currency," or measure of privacy, with which to work.



#### **Useful Databases that Teach**

- Database teaches that smoking causes cancer.
  - Smoker S's insurance premiums rise.
  - Premiums rise even if S not in database!
- Learning that smoking causes cancer is the whole point.
  - Smoker S enrolls in a smoking cessation program.
- Differential privacy: limit harms to the teachings, not participation

The outcome of any analysis is essentially equally likely, independent of whether any individual joins, or refrains from joining, the database.



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The likelihood of any possible harm to ME is essentially independent of whether I join, or refrain from joining, the database.



#### **Useful Databases that Teach**

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High premiums, busted, purchases revealed to co-worker... Essentially equally likely when I'm in as when I'm out



M gives  $\epsilon$ -differential privacy if for all pairs of data sets D, D' differing in one element, and all subsets C of possible outputs

 $\Pr[M(D) \in \mathcal{C}] \le e \uparrow \epsilon \Pr[M(D \uparrow ) \in \mathcal{C}]$ 

Randomness introduced by M



M gives  $\epsilon$ -differential privacy if for all pairs of data sets D, D' differing in one element, and all subsets C of possible outputs

 $\Pr[M(D) \in \mathcal{C}] \le (1+\epsilon) \Pr[M(D \uparrow^{\prime}) \in \mathcal{C}]$ 

Randomness introduced by M

If a bad event is very unlikely when I'm not in dataset (\( \nu \)) then it is still very unlikely when I am (\( \nu \))



C gives  $\epsilon$ -differential privacy if for all pairs of data sets D, D' differing in one element, and all subsets S of possible outputs

 $\Pr[\mathcal{C}(D) \in S] \le (1+\epsilon) \Pr[\mathcal{C}(D^{\uparrow}) \in S]$ 

Randomness introduced by M

If a bad event is very unlikely when I'm not in dataset (D) then it is still very unlikely when I am (D)

Impossible to know the actual probabilities of bad events. Can still control change in risk due to joining the database.



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### Differential Privacy

- Nuanced measure of privacy loss
  - Captures cumulative harm over multiple uses, multiple databases

- Adversary's background knowledge is irrelevant
  - Immune to re-identification attacks, etc.

- "Programmable"
  - Construct complicated private analyses from simple private building blocks

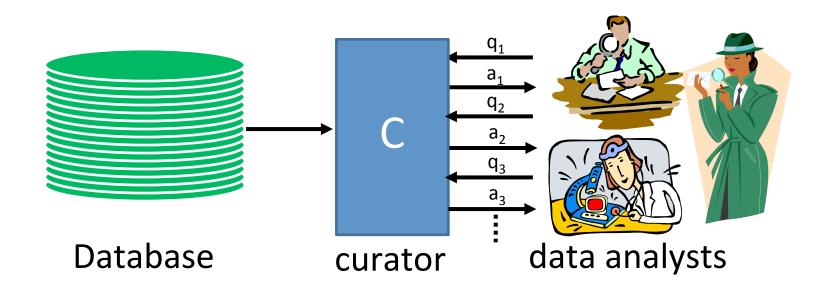


#### Recall: Fundamental Law



"Overly accurate" estimates of "too many" statistics is blatantly non-private

## **Answer Only Questions Asked**

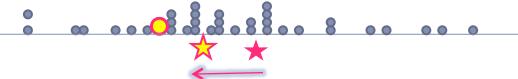




#### Intuition

- Want to compute f(D)
- ▶ Adding pulls f(D1')
  - Add random noise to obscure difference

$$f(D)$$
 vs  $f(D1')$ 



#### Intuition

- Want to compute f(D)
- ▶ Adding pulls f(D1')
  - Add random noise to obscure difference  $|f(D)-f(D)'|/\epsilon$

Algorithms, geometry, learning theory, complexity theory, cryptography, statistics, machine learning, programming languages, verification, databases, economics,...



### Not a Panacea

Fundamental Law of Information Recovery still holds





### Challenge: The Meaning of Loss

- Sometimes the theory gives exactly the right answer
  - Large loss in differential privacy translates to "obvious" real life privacy breach, under circumstances known to be plausible

#### Other times?

Do all large losses translate to such realizable privacy breaches, or is the theory too pessimistic?

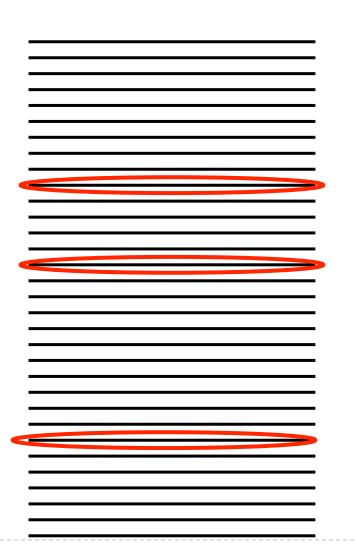


### Policy Recommendation

- Publish all Epsilons!
  - ▶ Penalize when  $\epsilon$ = ∞

Combines motivation for data breach notification statutes and environmental laws requiring disclosures of toxic releases with an incentive to start using (minimal) differential privacy

### "Just a Few"?





Randomly choose a few rows; Publish in entirety.

OK?



#### **Fundamental Law**

- There is a (LARGE) set of statistics, S
  - An analyst having even a remotely accurate estimate of EVERY statistic in S can completely violate any reasonable notion of privacy



Must be very inaccurate on some statistic in S

"Overly accurate" estimates of "too many" statistics is blatantly non-private

- There is a very simple way of designing small sets of statistics, T
  - An analyst having estimates of 80% of the statistics in T that beat the sampling error can completely violate any reasonable notion of privacy
- DinurNissim03; DworkMcSherryTalwar07; DworkYekhanin08, De12, MuthukrishnanNikolov12,...