Lecture 3 Semiconductor Physics (II) Carrier Transport

Outline

- Thermal Motion
- Carrier Drift
- Carrier Diffusion

Reading Assignment: Howe and Sodini; Chapter 2, Sect. 2.4-2.6

1. Thermal Motion

In thermal equilibrium, carriers are not sitting still:

- Undergo collisions with vibrating Si atoms (*Brownian motion*)
- Electrostatically interact with each other and with ionized (charged) dopants



Characteristic time constant of thermal motion: ⇒ mean free time between collisions

$\tau_c \equiv collison time [s]$

In between collisions, carriers acquire high velocity:

$\mathbf{v}_{\mathbf{th}} \equiv \mathbf{thermal velocity} [\mathbf{cms}^{-1}]$

.... but get nowhere!



Characteristic length of thermal motion:

 $\lambda \equiv mean free path [cm]$

$$\lambda = \mathbf{v_{th}} \tau_{\mathbf{c}}$$

Put numbers for Si at room temperature: $\tau_c \approx 10^{-13} s$ $v_{th} \approx 10^7 cm s^{-1}$ $\Rightarrow \lambda \approx 0.01 \ \mu m$

For reference, state-of-the-art production MOSFET: $L_g \approx 0.1 \ \mu m$

⇒ Carriers undergo many collisions as they travel through devices

2. Carrier Drift

Apply electric field to semiconductor:

 $E \equiv electric field [V cm^{-1}]$







Between collisions, carriers accelerate in the direction of the electrostatic field:

$$\mathbf{v}(\mathbf{t}) = \mathbf{a} \bullet \mathbf{t} = \pm \frac{\mathbf{q}\mathbf{E}}{\mathbf{m}_{\mathbf{n},\mathbf{p}}} \mathbf{t}$$

But there is (on the average) a collision every τ_c and the velocity is randomized:



The average net velocity in direction of the field:

$$\overline{\mathbf{v}} = \mathbf{v_d} = \pm \frac{\mathbf{qE}}{2\mathbf{m_{n,p}}} \tau_{\mathbf{c}} = \pm \frac{\mathbf{q\tau_c}}{2\mathbf{m_{n,p}}} \mathbf{E}$$

This is called **drift velocity** [cm s⁻¹]

Define:

$$\mu_{\mathbf{n},\mathbf{p}} = \frac{\mathbf{q}\,\tau_{\mathbf{c}}}{2\mathbf{m}_{\mathbf{n},\mathbf{p}}} \equiv \mathbf{mobility}\,[\mathbf{cm}^2\mathbf{V}^{-1}\mathbf{s}^{-1}]$$

Then, for electrons:

$$\mathbf{v}_{\mathbf{dn}} = -\mu_{\mathbf{n}}\mathbf{E}$$

and for holes:

$$\mathbf{v_{dp}} = \mu_{\mathbf{p}} \mathbf{E}$$

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Mobility - is a measure of *ease* of carrier drift

- If $\tau_c \uparrow$, longer time between collisions $\Rightarrow \mu \uparrow$
- If m \downarrow , "lighter" particle $\Rightarrow \mu \uparrow$

At room temperature, mobility in Si depends on doping:



- For low doping level, μ is limited by collisions with lattice. As Temp ->INCREASES; μ-> DECREASES
- For medium doping and high doping level, μ limited by collisions with ionized impurities
- Holes "heavier" than electrons
 - For same doping level, $\mu_n > \mu_p$

Drift Current

Net velocity of charged particles \Rightarrow electric current:

Drift current density

 ∞ carrier drift velocity ∞ carrier concentration ∞ carrier charge

Drift current densities:

$$J_n^{drift} = -qnv_{dn} = qn\mu_n E$$
$$J_p^{drift} = qpv_{dp} = qp\mu_p E$$

Check signs:



Total Drift Current Density :

$$\mathbf{J}^{drift} = \mathbf{J}_{n}^{drift} + \mathbf{J}_{p}^{drift} = \mathbf{q} \left(\mathbf{n} \boldsymbol{\mu}_{n} + \mathbf{p} \boldsymbol{\mu}_{p} \right) \mathbf{E}$$

Has the form of Ohm's Law

$$J = \sigma E = \frac{E}{\rho}$$

Where:

$$\sigma \equiv \text{conductivity} [\Omega^{-1} \bullet \text{cm}^{-1}]$$

$$\rho \equiv \text{resistivity} [\Omega \bullet \text{cm}]$$

Then:

$$\sigma = \frac{1}{\rho} = q \left(n \mu_n + p \mu_p \right)$$

Resistivity is commonly used to specify the doping level

• In n-type semiconductor:

$$\rho_{\mathbf{n}} \approx \frac{1}{\mathbf{q} \mathbf{N}_{\mathbf{d}} \boldsymbol{\mu}_{\mathbf{n}}}$$

• In p-type semiconductor:





Numerical Example:

Si with $N_d = 3 \times 10^{16} \text{ cm}^{-3}$ at room temperature $\mu_n \approx 1000 \ cm^2 / V \bullet s$ $\rho_n \approx 0.21 \Omega \bullet cm$ $n \approx 3X10^{16} cm^{-3}$ Apply E = 1 kV/cm $|v_{dn}| \approx 10^6 cm/s \ll v_{th}$ $J_n^{drift} \approx qnv_{dn} = qn\mu_n E = \sigma E = \frac{E}{2}$ $J_n^{drift} \approx 4.8 \times 10^3 A / cm^2$

Time to drift through $L = 0.1 \ \mu m$

$$t_d = \frac{L}{v_{dn}} = 10 \, ps$$

3. Carrier Diffusion

<u>**Diffusion**</u> = particle movement (flux) in response to concentration gradient



Elements of diffusion:

- A medium (*Si Crystal*)
- A gradient of particles (*electrons and holes*) inside the medium
- Collisions between particles and medium send particles off in random directions
 - Overall result is to erase gradient

Fick's first law-Key diffusion relationship

Diffusion flux ∞ - concentration gradient

Flux = number of particles crossing a unit area per unit time $[cm^{-2} \cdot s^{-1}]$

For Electrons:

$$\mathbf{F_n} = -\mathbf{D_n} \frac{\mathbf{dn}}{\mathbf{dx}}$$

For Holes:

$$\mathbf{F}_{\mathbf{p}} = -\mathbf{D}_{\mathbf{p}} \frac{\mathbf{d}\mathbf{p}}{\mathbf{d}\mathbf{x}}$$

 $\mathbf{D_n} \equiv$ electron diffusion coefficient [cm² s⁻¹] $\mathbf{D_p} \equiv$ hole diffusion coefficient [cm² s⁻¹]

D measures the <u>ease</u> of carrier diffusion in response to a concentration gradient: $D \uparrow \Rightarrow F^{diff} \uparrow$

D limited by vibration of lattice atoms and ionized dopants.

Diffusion Current

Diffusion current density =charge × carrier flux

$$J_n^{diff} = qD_n \frac{dn}{dx}$$
$$J_p^{diff} = -qD_p \frac{dp}{dx}$$

Check signs:



Einstein relation

At the core of drift and diffusion is same physics: collisions among particles and medium atoms \Rightarrow there should be a relationship between D and μ

Einstein relation [will not derive in 6.012]

$$\frac{D}{\mu}=\frac{kT}{q}$$

In semiconductors:

<u>D</u> _n	=	<u>kT</u>	=	D _p
$\mu_{\mathbf{n}}$		q		$\mu_{\mathbf{p}}$

 $kT/q \equiv$ thermal voltage

At room temperature:

$$\frac{\mathbf{kT}}{\mathbf{q}} \approx 25 \,\mathbf{mV}$$

For example: for $N_d = 3 \times 10^{16} \text{ cm}^{-3}$

$$\mu_n \approx 1000 \, cm^2 \, / \, V \bullet s \quad \Rightarrow D_n \approx 25 \, cm^2 \, / \, s$$
$$\mu_p \approx 400 \, cm^2 \, / \, V \bullet s \quad \Rightarrow D_p \approx 10 \, cm^2 \, / \, s$$

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Total Current Density

In general, total current can flow by drift and diffusion separately. **Total current density:**

$$\mathbf{J}_{n} = \mathbf{J}_{n}^{drift} + \mathbf{J}_{n}^{diff} = \mathbf{q}\mathbf{n}\mu_{n}\mathbf{E} + \mathbf{q}\mathbf{D}_{n}\frac{\mathbf{d}\mathbf{n}}{\mathbf{d}\mathbf{x}}$$
$$\mathbf{J}_{p} = \mathbf{J}_{p}^{drift} + \mathbf{J}_{p}^{diff} = \mathbf{q}\mathbf{p}\mu_{p}\mathbf{E} - \mathbf{q}\mathbf{D}_{p}\frac{\mathbf{d}\mathbf{p}}{\mathbf{d}\mathbf{x}}$$

 $\mathbf{J}_{total} = \mathbf{J}_{n} + \mathbf{J}_{p}$

What did we learn today?

Summary of Key Concepts

• Electrons and holes in semiconductors are mobile and charged

 $- \Rightarrow$ Carriers of electrical current!

• **Drift current**: produced by electric field

$$\mathbf{J}^{\mathbf{drift}} \propto \mathbf{E} \quad \mathbf{J}^{\mathbf{drift}} \propto rac{\mathbf{d}\phi}{\mathbf{dx}}$$

• *Diffusion current*: produced by concentration gradient

$$J^{diffusion} \propto \frac{dn}{dx}, \frac{dp}{dx}$$

- Diffusion and drift currents are sizeable in modern devices
- Carriers move fast in response to fields and gradients