Lecture 23

Frequency Response of Amplifiers (III) OTHER AMPLIFIER STAGES

Outline

- 1. Frequency Response of the Common-Drain Amplifier
- 2. Frequency Response of the Common-Gate Amplifier

Reading Assignment:

Howe and Sodini, Chapter 10, Sections 10-5-10.6

1. Frequency Response of the Common-Drain Amplifier



Characteristics of CD Amplifier:

- Voltage gain ≈ 1
- High input resistance
- Low output resistance
- \Rightarrow Good voltage buffer



Low Frequency Analysis Using 2-Port Model



Capacitors -open circuit

$$A_{vo} = \left(\frac{R_{in}}{R_S + R_{in}}\right) (1) \left(\frac{R_L}{R_L + R_{out}}\right)$$
$$\approx \frac{g_m R_L}{1 + g_m R_L} \le 1$$

In the calculation of the intrinsic voltage gain we assume that $r_0 ||r_{oc}$ was large. That is why we do not have $R_L || r_0 ||r_{oc}$

High Frequency Analysis Using 2-Port Model - Add capacitors



Use Miller Approximation

$$A_{vC_{gs}} = \frac{R_L}{R_{out} + R_L} = \frac{g_m R_L}{1 + g_m R_L}$$
$$= C_{vL} \left(1 - \frac{g_m R_L}{1 - g_m R_L}\right) = \frac{C_{gs}}{C_{gs}}$$

$$C_M = C_{gs} \left(1 - A_{vC_{gs}} \right) = C_{gs} \left(1 - \frac{g_m R_L}{1 + g_m R_L} \right) = \frac{c_{gs}}{1 + g_m R_L}$$

Total capacitance at input

$$C_T = C_{gs} \left(1 - \frac{g_m R_L}{1 + g_m R_L} \right) + C_{gd}$$

$$R_T = R_S || R_{in} = R_S$$

Add time constant due to C_{db} capacitance at output

$$R_{C_{db}} = R_{out} ||R_L| = \frac{R_{out}R_L}{R_{out} + R_L} = \frac{R_L}{1 + g_m R_L}$$

Frequency Response of Common-Drain Amplifier



$$\omega_{3dB} \approx \frac{1}{R_s \left(\frac{C_{gs}}{1 + g_m R_L} + C_{gd}\right) + C_{db} \frac{R_L}{1 + g_m R_L}}$$

If R_s is not too high, bandwidth can be rather high and approach ω_T .

2. Frequency Response of the Common-Gate Amplifier



Characteristics of CG Amplifier:

- Current gain ≈ 1
- Low input resistance
- High output resistance
- \Rightarrow Good current buffer

High Frequency Small Signal Model



Could use OTC to solve for bandwidth.

To estimate bandwidth it is easier to use the 2-port models.

High-frequency small-signal 2-port model Assume backgate is shorted to source



Low frequency transfer function:

$$A_{io} = \frac{i_{out}}{i_s} = \left(\frac{R_S}{R_{in} + R_S}\right)(1) \left(\frac{R_{out}}{R_L + R_{out}}\right)$$

Use OTC to find ω_{3dB} :

The venin resistance across C_{gs}

$$R_{TC_{gs}} = R_S \parallel R_{in} = R_S \parallel (1/g_m)$$

The venin resistance across C_{gd}

$$R_{TC_{gd}} = R_{out} || R_L = ((r_o + g_m r_o R_S) || r_{oc}) || R_L$$

High-frequency small-signal 2-port model con't



Open circuit time constants:

$$\tau_{C_{gs}} = (R_S \parallel (1/g_m))C_{gs}$$

$$\tau_{C_{gd}} = (((r_o + g_m r_o R_S) \parallel r_{oc})) \parallel R_L)C_{gd}$$

Summing the open circuit time constants:

$$\omega_{3dB} = 1 / \left[\left(R_{S} \| (1/g_{m}) \right) C_{gs} + \left(\left((r_{o} + g_{m} r_{o} R_{S}) \| r_{oc} \right) \| R_{L} \right) C_{gd} \right]$$

If R_L is not too high, bandwidth can be rather high and approach ω_T .

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What did we learn today?

Summary of Key Concepts

- Common-drain amplifier:
 - Voltage gain \approx 1, *Miller Effect* nearly completely eliminates the effect of C_{gs}
 - If R_S is not too high, CD amplifier has high bandwidth
- Common-gate amplifier
 - No Miller Effect because there is no feedback capacitor
 - If R_L is not too high, CG amplifier has high bandwidth
- R_S , R_L can affect bandwidth of amplifiers.